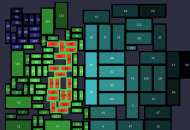
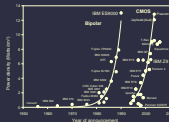
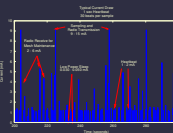
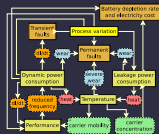


Digital Integrated Circuits – EECS 312

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Review

- When are the advantages and disadvantages of fixed-voltage charging?
- When are the advantages and disadvantages of fixed-current charging?
- In what situation is each of the following models important?
 - Ideal.
 - C .
 - RC .
 - RLC .
- What are di/dt effects? Under what circumstances do they cause the most trouble?

Derive and explain.

Lecture plan

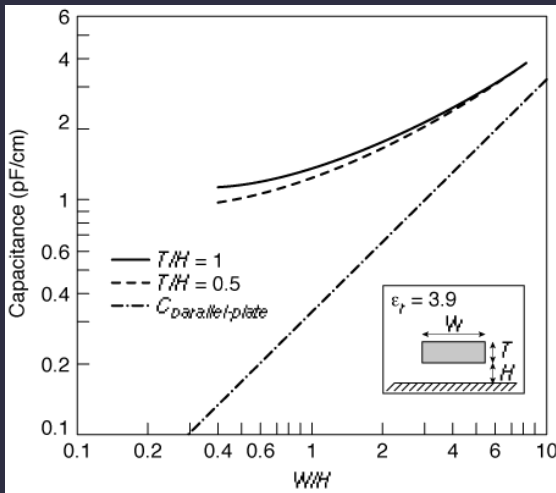
1. Interconnect: Rent's rule and coupling capacitance
2. Elmore delay modeling
3. Logic design
4. Homework

Rent's rule

$$T = ak^p$$

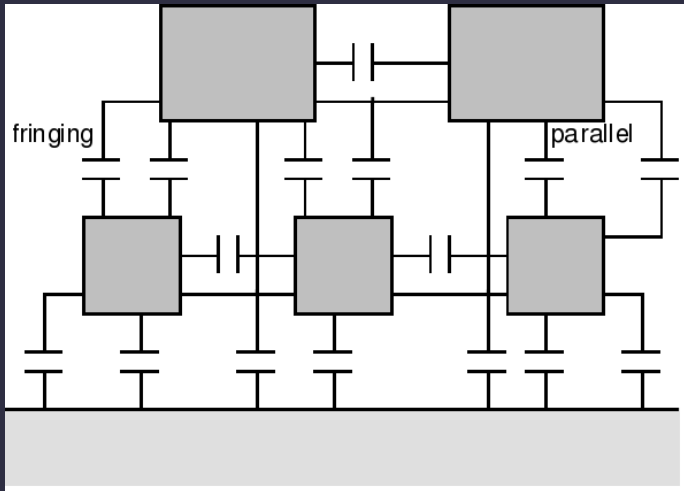
- T : Number of terminals.
- a : Average number of terminals per block.
- k : Number of blocks within chip.
- p : Rent's exponent, ≤ 1 , generally around 0.7.

Fringe vs. parallel plate capacitance

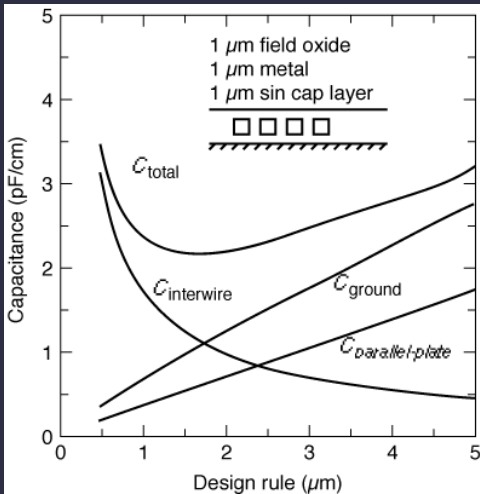


Plot of C_{total} for different gap ratios.

Inter-wire capacitance



Impact of inter-wire capacitance



Wire resistance

- $R = \frac{\rho L}{HW}$.
- Consider fixed-height, fixed- ρ square material, i.e., $L/W = 1$.
- $R = \frac{\rho}{H}$.

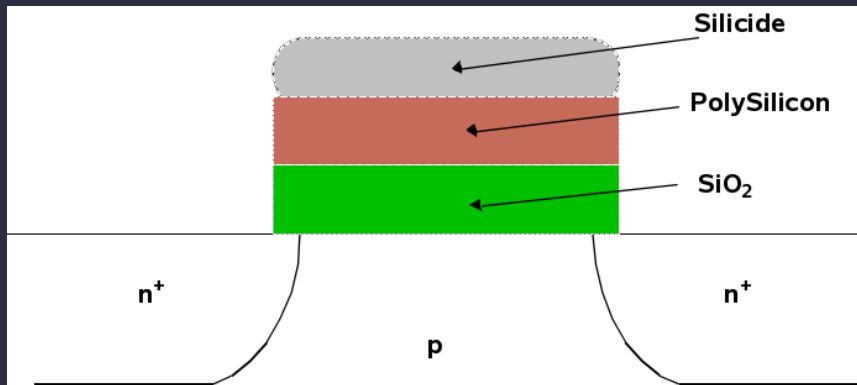
Interconnect resistance

Material	ρ (Ω m) $\times 10^{-8}$
Silver	1.6
Copper	1.7
Gold	2.2
Aluminum	2.7
Tungsten	5.5

Reducing resistance

- Higher interconnect aspect ratios
- Material selection
 - Copper
 - Silicides
 - Carbon nanotubes
- Structural changes
 - More interconnect layers
 - 3-D integration

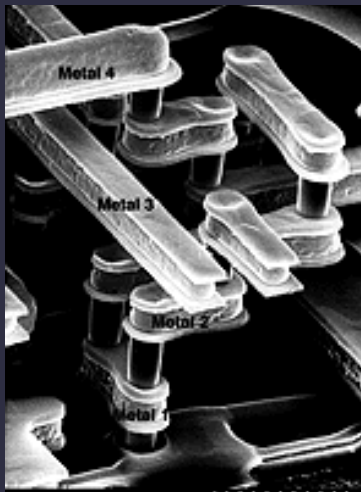
Silicides



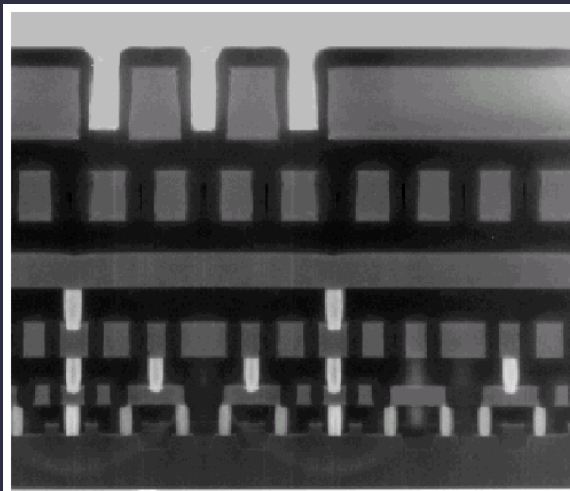
Resistances

Material	Sheet resistance (Ω/\square)
n- or p-well diffusion	1,000–1,500
n ⁺ or p ⁺ diffusion	50–150
silicided n ⁺ or p ⁺ diffusion	3–5
doped polysilicon	150–200
doped silicides polysilicon	4–5
Aluminum	0.05–0.1

Multi-layer interconnect



Side view of interconnect



Interconnect summary

- It is important to know which interconnect model to use in which situation.
 - Ideal.
 - C .
 - RC .
 - RLC .
- dl/dt effects are particularly important in power delivery networks.
- Capacitive coupling complicates design.
- Cu and silicides can be used to reduce resistance.

Lecture plan

1. Interconnect: Rent's rule and coupling capacitance
2. Elmore delay modeling
3. Logic design
4. Homework

Delay modeling

- Single-node lumped model inaccurate.
- Full detailed accurate model intractable for manual analysis and slow for automated analysis.
- Elmore delay model permits rapid analysis with often adequate accuracy.

Elmore delay

Problem definition

- Goal: Determine τ for RC path.
- Note: Source node is implicit.
- C_i : Self-capacitance of node i .
- R_{ij} : Path resistance from source to node i .
- R_{ik} : Shared resistance from source to both nodes i and k .

$$\tau_i = \sum_{k=1}^N C_k R_{ik}$$

Derive and explain.

Special case: RC chains

- Consider π network.
- $\tau_n = \sum_{i=1}^n C_i \sum_{j=1}^i R_j$.
- Use homogeneous discretization.
- $\forall_{i=2}^N C_i = C_1$

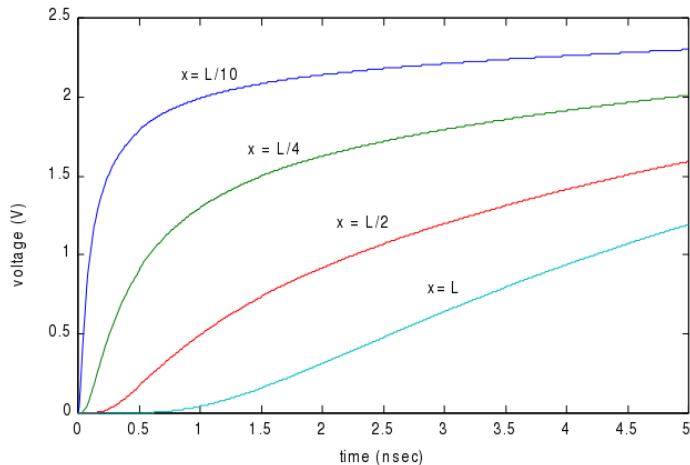
$$\begin{aligned}\tau &= \sum_{k=1}^N CR_{nk} \\ &= \frac{L}{N} C \frac{L}{N} r \frac{N(N+1)}{2} \\ &= rcL^2 \frac{N+1}{2N}\end{aligned}$$

What if $N \rightarrow \infty$? $\tau \rightarrow rcL^2/2$.

Underlying continuous physical model

$$cr \frac{\delta V}{\delta t} = \frac{\delta^2 V}{\delta x^2}$$

Response to step function over time and space



Power delivery network considerations

- IR drop.
- di/dt effects.
- Location of parasitic inductance.
- Methods to correct power delivery network non-idealities.

Simplifying assumptions

- Ignore wire RC delay when wire delay does not much exceed that of the driving gate, i.e.,

$$L_{crit} \gg \sqrt{\frac{t_{p,gate}}{0.38rc}}$$

- Ignore wire RC when rise time greater than RC delay.
- Ignore for high-resistance wires: $R > 0.2C$.
- Ignore when time of flight is large compared to rise or fall time:
 $t_{rise,fall} < 2.5t_{flight}$.

Elmore delay summary

- Pick simplest model for intended purpose: C , RC , or RLC .
- Capacitive coupling complicates timing analysis.
- Transition direction impacts C magnitude in simplified ground-cap model.
- Learn Elmore delay. It is a good first-order approximation of network delay.

Lecture plan

1. Interconnect: Rent's rule and coupling capacitance
2. Elmore delay modeling
3. Logic design
4. Homework

Static CMOS design styles and components

- Logic gates
- Switch-based design
- MUX
- DEMUX
- Encoder
- Decoder

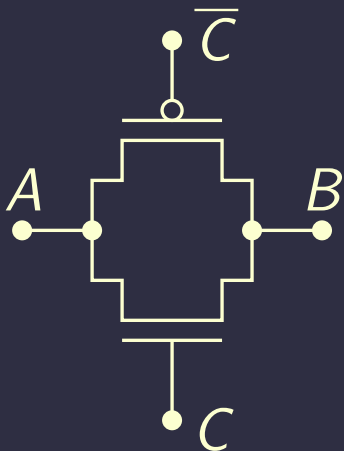
Transistor sizing review

- Goal: equal τ for worst-case pull-up and pull-down paths.
- Observations
 - Adding duplicate parallel path halves resistance.
 - Adding duplicate series path doubles resistance.
 - Doubling width halves resistance.
- Consider logic gate examples.

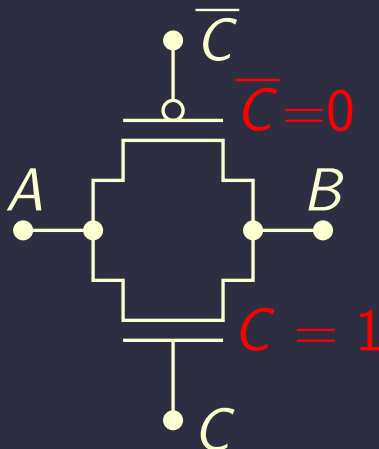
Section outline

3. Logic design
 - Switch-based design

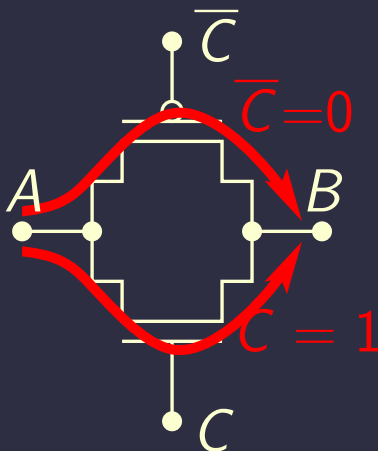
CMOS transmission gate (TG)



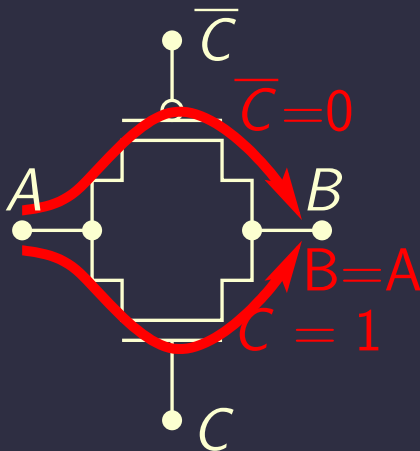
CMOS transmission gate (TG)



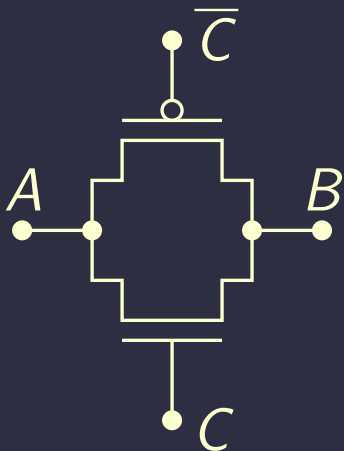
CMOS transmission gate (TG)



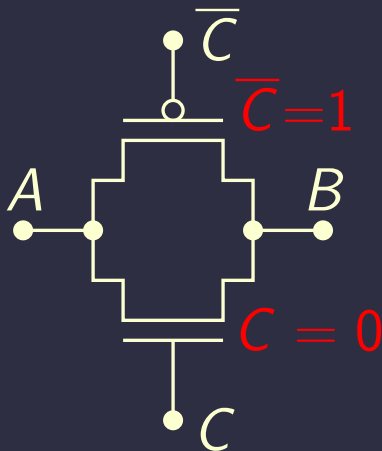
CMOS transmission gate (TG)



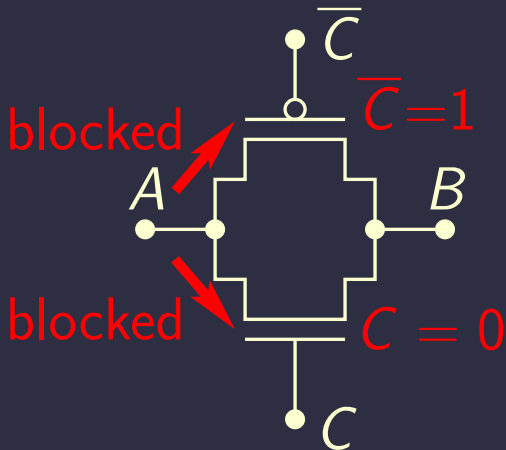
CMOS transmission gate (TG)



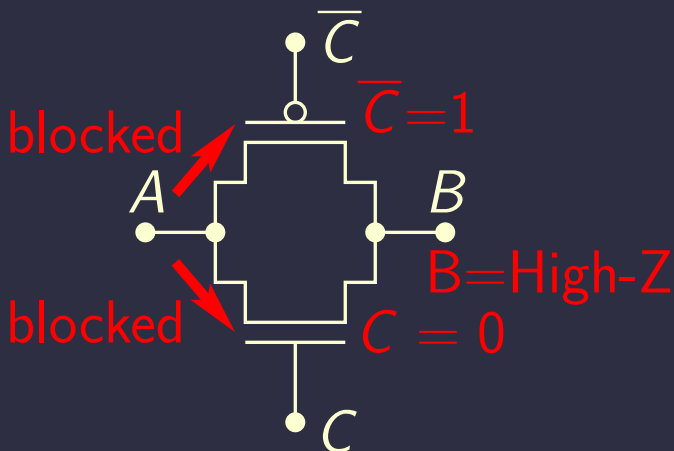
CMOS transmission gate (TG)



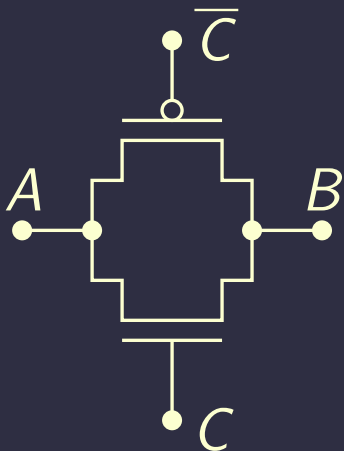
CMOS transmission gate (TG)



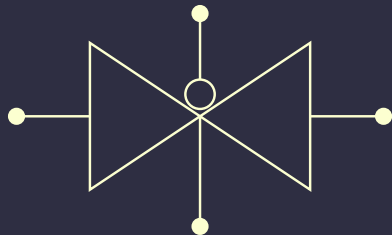
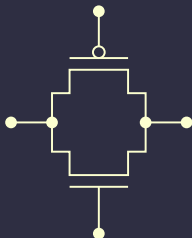
CMOS transmission gate (TG)



CMOS transmission gate (TG)



Other TG diagram



Multiplexer (MUX) definitions

- Also called *selectors*
- 2^n inputs
- n control lines
- One output

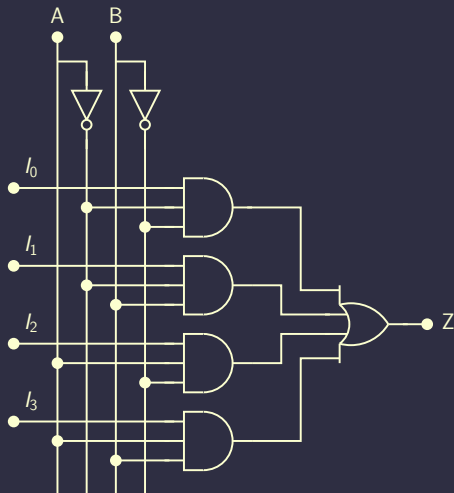
MUX functional table

C	Z
0	I_0
1	I_1

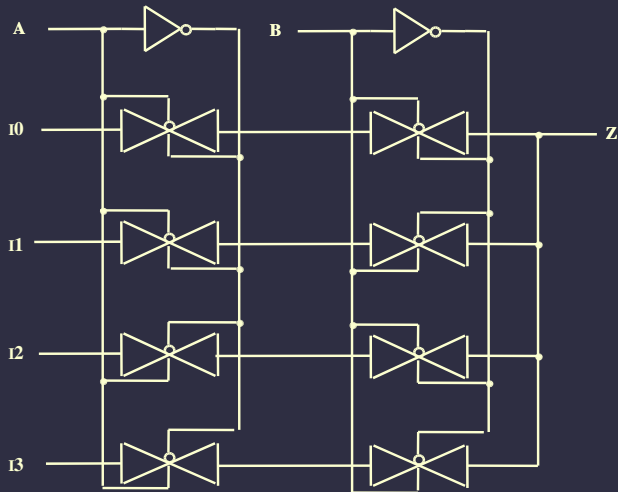
MUX truth table

I_1	I_0	C	Z
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

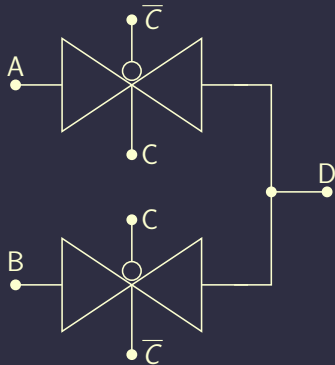
MUX using logic gates



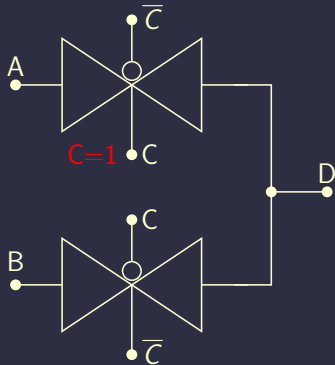
MUX using TGs



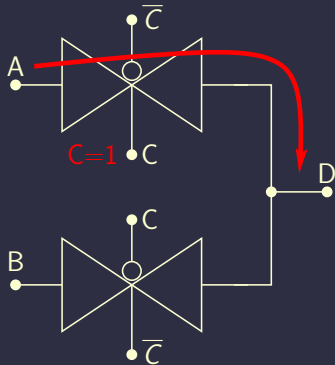
MUX



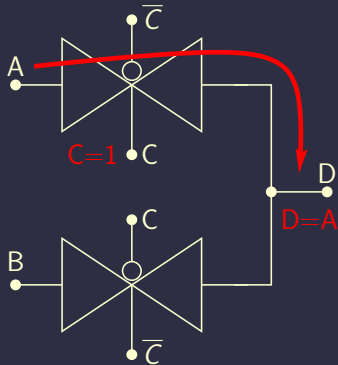
MUX



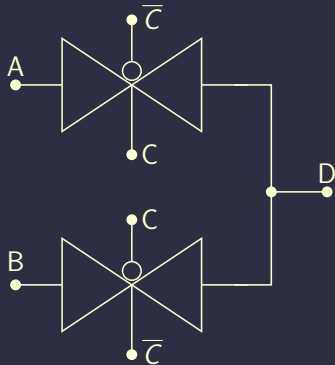
MUX



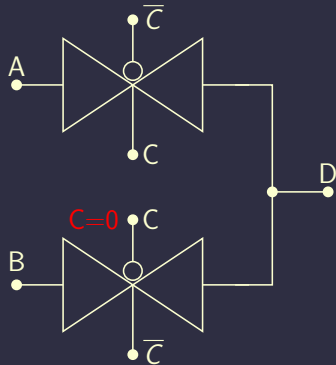
MUX



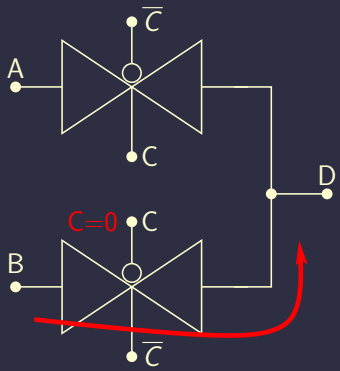
MUX



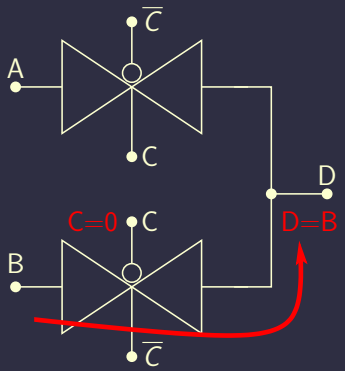
MUX



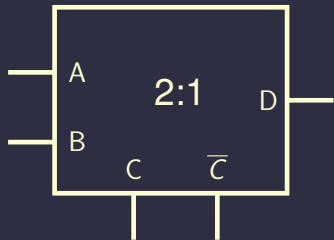
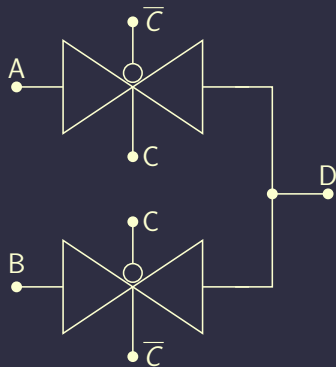
MUX



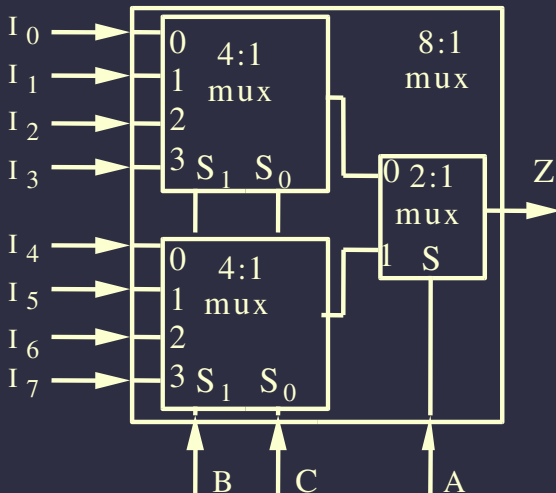
MUX



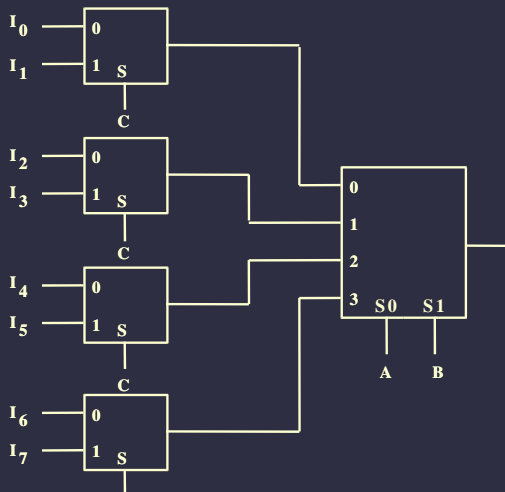
MUX



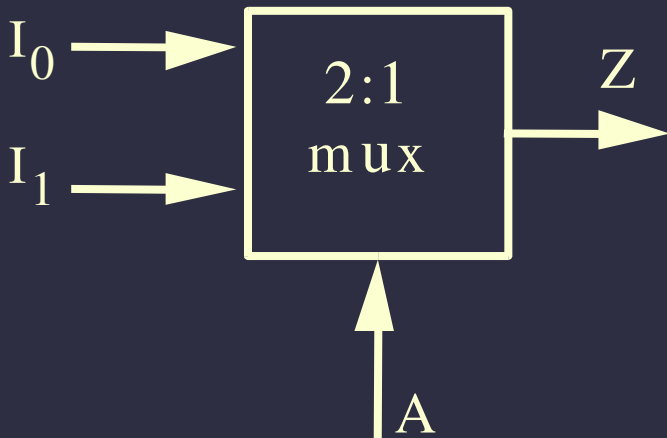
Hierarchical MUX implementation



Alternative hierarchical MUX implementation

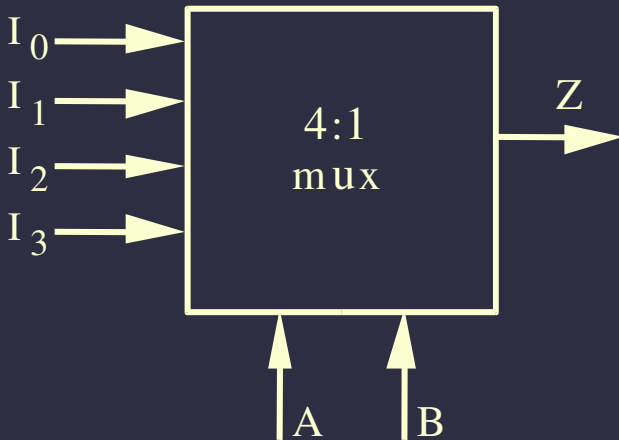


MUX examples



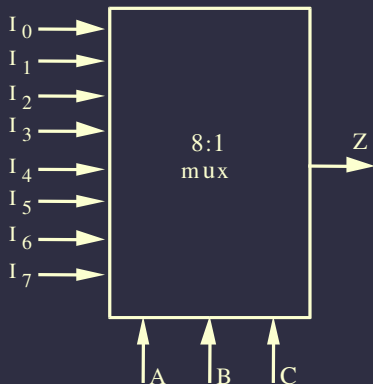
$$Z = \bar{A}I_0 + AI_1$$

MUX examples



$$Z = \bar{A}\bar{B}I_0 + \bar{A}BI_1 + A\bar{B}I_2 + ABI_3$$

MUX examples



$$Z = \bar{A}\bar{B}\bar{C}I_0 + \bar{A}\bar{B}CI_1 + \bar{A}B\bar{C}I_2 + \bar{A}BCI_3 + \\ AB\bar{C}I_4 + AB CI_5 + ABC\bar{C}I_6 + ABCI_7$$

MUX properties

- A $2^n : 1$ MUX can implement any function of n variables
- A $2^{n-1} : 1$ can also be used
 - Use remaining variable as an input to the MUX

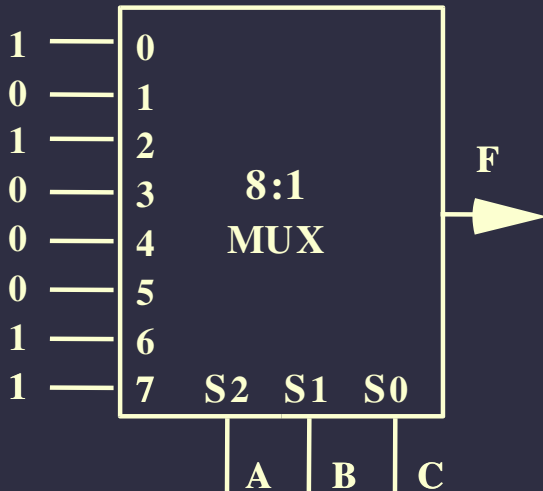
MUX example

$$\begin{aligned} F(A, B, C) &= \sum(0, 2, 6, 7) \\ &= \overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + AB\overline{C} + ABC \end{aligned}$$

Truth table

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Lookup table implementation



MUX example

$$\begin{aligned} F(A, B, C) &= \sum(0, 2, 6, 7) \\ &= \overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + AB\overline{C} + ABC \end{aligned}$$

Therefore,

$$\overline{A}\overline{B} \rightarrow F = \overline{C}$$

$$\overline{A}B \rightarrow F = \overline{C}$$

$$A\overline{B} \rightarrow F = 0$$

$$AB \rightarrow F = 1$$

Truth table

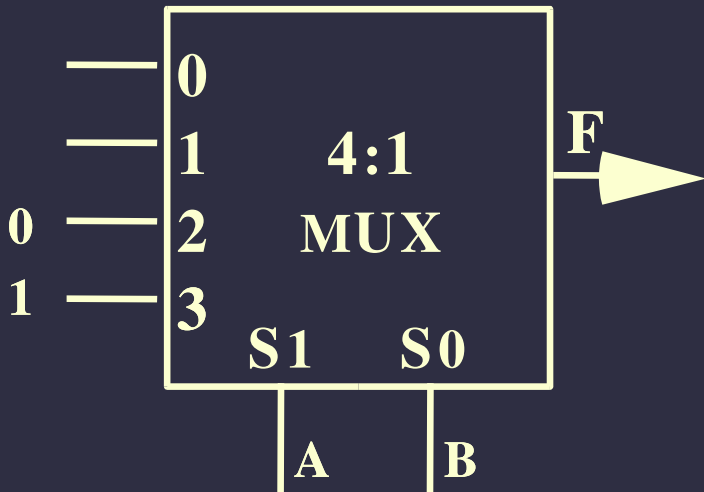
A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Truth table

A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

$$F = \overline{C}$$

Lookup table implementation



Logic design summary

- Logic gate, transmission gate, and pass transistor design each have applications.
- MUX-based design provides a good starting point for transmission gate and pass transistor based design.

Examples

Instead of flying through a bunch of slides, let's try examples.

- $f(a) = a$.
- $f(a) = \bar{a}$
- $f(a, b) = a\bar{b}$
- $f(a, b) = ab$ (Check Figure 6-33 in J. Rabaey, A. Chandrakasan, and B. Nikolic. *Digital Integrated Circuits: A Design Perspective*. Prentice-Hall, second edition, 2003!)
- $f(a, b, c) = ab + \bar{b}c$ (try both ways).

Derive and explain.

Upcoming topics

- Alternative logic design styles.
- Latches and flip-flops.
- Memories.

Lecture plan

1. Interconnect: Rent's rule and coupling capacitance
2. Elmore delay modeling
3. Logic design
4. Homework

Homework assignment

- 22 October: Read sections 4.4.1, 4.4.4, and 9.3.3 in J. Rabaey, A. Chandrakasan, and B. Nikolic. *Digital Integrated Circuits: A Design Perspective*. Prentice-Hall, second edition, 2003.
- 24 October: Read sections 6.2.2 and 6.2.3 in J. Rabaey, A. Chandrakasan, and B. Nikolic. *Digital Integrated Circuits: A Design Perspective*. Prentice-Hall, second edition, 2003.
- 25 October: Lab 3.
- 29 October: Homework 3.