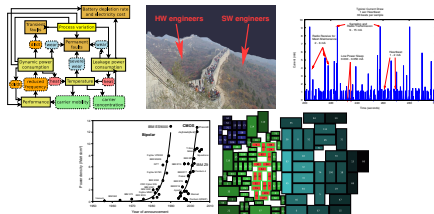


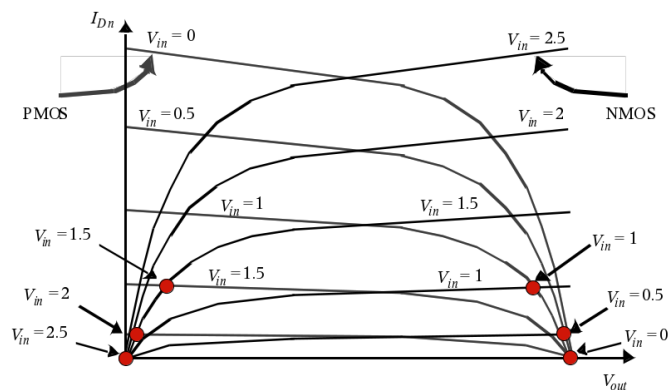
Digital Integrated Circuits – EECS 312

<http://robertdick.org/eecs312/>

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Review I



2

Review II

- How can the transfer curve for an inverter be derived from the I-V curves of the MOSFETs comprising it?
- What useful property relevant to the inverter load curve diagram holds in steady state but not when transients are considered?
- Is the inverter load curve diagram useful for analyzing dynamic systems?

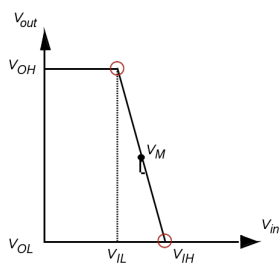
Midterm exam

- May cover anything up to and including 3 October.
- Make sure you did the assigned reading.
- Look though all the on-line slides for anything surprising.
- Review lab and homework assignments.
- If you want to study with other students, please use mailing list to find partners.
- Posted old exams to website.
- No class on Tuesday.

3

4

V_{IH} and V_{IL}



$$V_{IH} - V_{IL} = -\frac{V_{OH} - V_{OL}}{g} = \frac{-V_{DD}}{g} \quad (1)$$

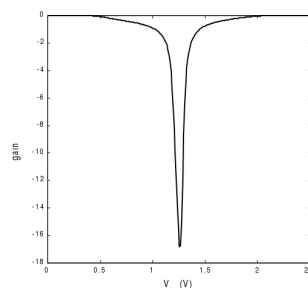
$$V_{IH} = V_M - \frac{V_M}{g} \quad (2)$$

$$V_{IL} = V_M + \frac{V_{DD} - V_M}{g} \quad (3)$$

$$NM_H = V_{DD} - V_{IH} \quad (4)$$

$$NM_L = V_{IL} \quad (5)$$

Inverter gain



Can find gain by taking $\sigma V_{out} / \sigma V_{in}$ at V_M .

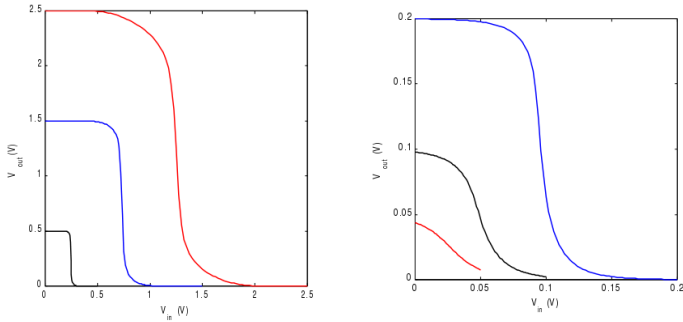
$$g = -\frac{1}{I_D(V_M)} \frac{k_n V_{DSATn} + k_p V_{DSATp}}{\lambda_n - \lambda_p} \quad (1)$$

$$g \approx \frac{1+r}{(V_M - V_{Tn} - \frac{V_{DSATn}}{2})(\lambda_n - \lambda_p)} \quad (2)$$

6

7

Change in transfer curve (and gain) with V_{DD}



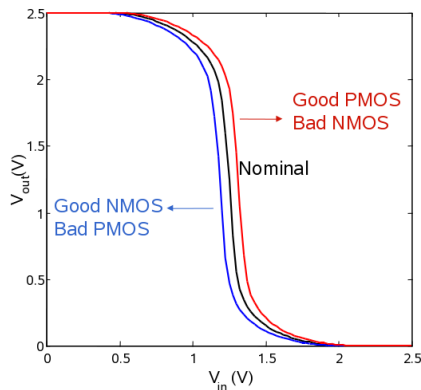
8

Subthreshold operation

- Higher gain.
- Lower current.
- Increased sensitivity to intrinsic noise.
- Increased sensitivity to fixed external noise.
 - $\frac{\alpha kT}{q}$

9

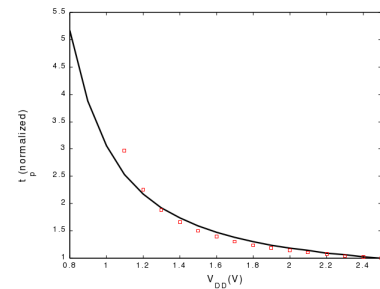
Impact of process variation on inverter transfer function



10

Inverter performance

- Recall inverter propagation delay expression: $t_p = 0.69RC$.
- Either decrease R or decrease C .
- Effective R depends on V_{DD} .



11

Dependence of inverter delay on V_{DD} I

$$t_{pHL} = 0.69 \frac{3 C_L V_{DD}}{4 I_{DSATn}}$$

$$t_{pHL} = 0.52 \frac{L_n}{W_n k'_n V_{DSATn}} \frac{C_L V_{DD}}{(V_{DD} - V_{Tn} - V_{DSATn}/2)}$$

If $V_{DD} \gg V_{Tn} + V_{DSATn}/2$

$$t_{pHL} \approx 0.52 \frac{L_n}{W_n k'_n V_{DSATn}} \frac{C_L}{V_{DD}}$$

Why?

$$R_{eq} = \frac{1}{V_{DD}/2} \int_{V_{DD}/2}^{V_{DD}} \frac{V}{I_{DSAT}(1 + \lambda V)} dV \approx \frac{3}{4} \frac{V_{DD}}{I_{DSAT}} \left(1 - \frac{7}{9} \lambda V_{DD}\right)$$

12

Dependence of inverter delay on V_{DD} II

where

$$I_{DSAT} = k' \frac{W}{L} \left((V_{DD} - V_T) V_{DSAT} - \frac{V_{DSAT}^2}{2} \right)$$

Ignore channel length modulation factor λ .

13

Review

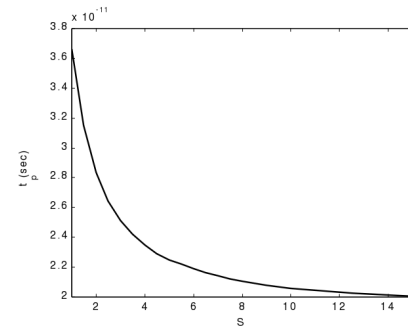
- Define noise margin and explain why it is a useful concept.
- What is V_M ?
- What influence does an asymmetric change in inverter MOSFET resistance have on the $V_{out}-V_{in}$ curve?
- What is inverter gain and how does it depend on V_{DD} ?
- What happens to inverter delay with decreasing V_{DD} ?

14

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Dependence of delay on width (R)



- Fix $R_L C_L$ and vary W .
- Eventually, self-loading dominates.

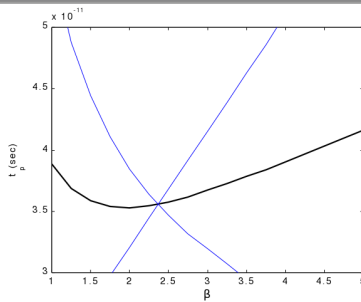
16

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Impact of W_p/W_n ratio

Warning: Broken concept, especially for short-chain analysis.



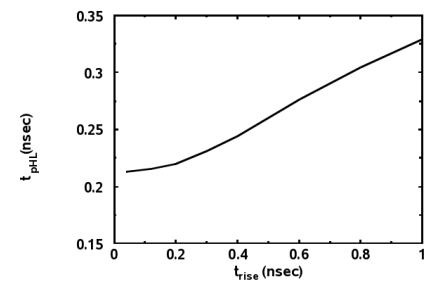
- $\beta = W_p/W_n$.
- $t_p = \frac{t_{pLH} + t_{pHL}}{2}$.

17

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Impact of rise time on delay



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Modeling rise time effects in inverter chains

$$t_p^i = t_{step}^i + \eta t_{step}^{i-1}$$

- t_{step}^i : Delay of gate i in response to step input function.
- η : Technology-dependent constant, generally near 0.25.

19

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Midterm exam I

- 1 Uses of digital systems.
- 2 History of digital computing devices. Impact of technology improvements on performance, power consumption, size, and reliability. Bipolar to CMOS move.
- 3 Power consumption equation and components of total power consumption. Check Slide 19 in lecture notes packet 2.
- 4 Requirements for devices to permit use in digital system. Regeneration/restoration.
- 5 MOSFET structure and layout.
- 6 Schematic capture, e.g., using Cadence software.
- 7 Resistance basics, and their application to MOSFET channels and metal wires.

21

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Midterm exam II

- 8 Basic logic gate and transmission gate structures.
- 9 NMOS, PMOS, and CMOS inverters.
- 10 Diode structure and operation. Drift and diffusion. Difference between charge carriers and stationary ions. Doping.
- 11 MOSFET operation. Change in conditions (especially I_D) with changing V_{GS} , V_{DS} , and V_{SB} . MOSFET models. Cutoff, pinch-off, and velocity saturation.
- 12 Subthreshold leakage and subthreshold operation.
- 13 Process variation definition and influence on circuit behavior.
- 14 High-level understanding of FinFET structure and reason for improved k .
- 15 Steps in fabrication process. Dual damascene process.
- 16 Understanding what design rules are.

22

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Midterm exam III

- 17 Packaging, MCMs, and board-level design. Implications of packaging and interconnect for performance.
- 18 Gate leakage. High- κ dielectric. See assigned article.
- 19 Transient diode and MOSFET behavior. Computing capacitances based on MOSFET structure and operating region.
- 20 Derivation from inverter transfer curve from MOSFET I-V curves. Impact of inverter asymmetry on V_M .
- 21 Noise margin definitions and purpose. Gain definition.

23

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Upcoming topics

- Inverter chains for driving large loads.
- Complex behavior in logic gate.

24

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Homework assignment

- 3 October: Read sections 5.3, 5.4.1, and 5.4.2 in J. Rabaey, A. Chandrakasan, and B. Nikolic. *Digital Integrated Circuits: A Design Perspective*. Prentice-Hall, second edition, 2003.
- 3 October: Lab 2.
- 10 October: Homework 2 (which will help in your preparation for the midterm exam).
- 10 October: Read sections 5.4, 5.5, 5.6, and 3.5 in J. Rabaey, A. Chandrakasan, and B. Nikolic. *Digital Integrated Circuits: A Design Perspective*. Prentice-Hall, second edition, 2003.

26

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