



# Towards Provably Safe and Secure Systems with Contract-Based Design

Embedded Systems Seminar  
19 Sept 2024

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**GM's Cruise Loses Its Self-Driving License in San Francisco After a Robotaxi Dragged a Person**

The California DMV says the company's autonomous taxis are "not safe" and that Cruise "misrepresented" safety information about its self-driving vehicle technology.

A Cruise, which is a driverless robot taxi, is seen during operation in San Francisco in July. PHOTOGRAPH: TAYFUN COSKUN/GETTY IMAGES

**SpaceX launched its giant new rocket but explosions end the second test flight**

Three minutes into flight, the separated booster exploded over the Gulf of Mexico. By then, its job was done, launching the rocket ship toward space.

**Honda, Acura Recalling 250,000 Vehicles over Engine Stall Risk**

About a quarter of a million 2016-2019 models are under recall for a connecting rod defect that can cause the engine to stall or not start, including the Pilot, Odyssey, Ridgeline, and Acura TLX and MDX.

BY LAURA SKY BROWN PUBLISHED: NOV 20, 2023

Improve how the Agency Engineering Domain operates over the entire NASA lifecycle by effectively managing complexity, reducing cost and schedule, and improving product integrity via **the integration of processes, digital tools, and techniques along with seamless flow of information throughout the engineering system development life-cycle** (concept development, design, testing and validation, manufacturing and operations)

— Terry Hill (NASA DT Digital Engineering Lead)

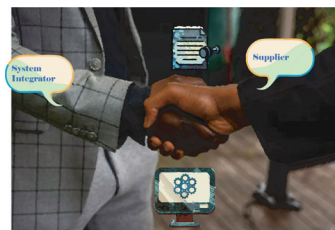


## Challenges in complex system design

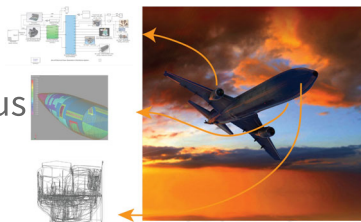
Multiple stakeholders



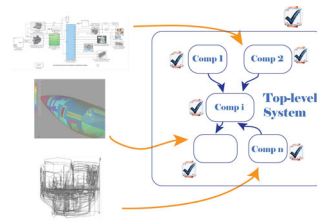
Complex supply chains



Heterogenous analyses



System integration



# Contracts

An algebra and a methodology to address

- System integration
  - Subsystems come from multiple OEMs
  - Integrate through **composition**
  - Find “missing components” through **quotient**
- Multiple viewpoints
  - At the same company, multiple groups work on same product
  - Merge them through **merging**

Albert Benveniste et al. Contracts for System Design. Foundations and Trends in Electronic Design Automation 2018  
Inigo Incer. The Algebra of Contracts, PhD thesis, UC Berkeley 2022

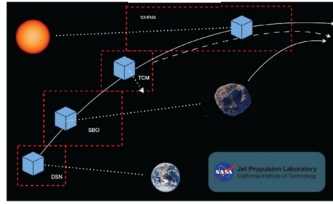
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The logo for Pacti.org features the word "pacti" in a dark blue, lowercase, sans-serif font. The letter "i" is stylized with an orange gear shape integrated into its vertical stem. Below "pacti" is ".ORG" in a dark blue, uppercase, sans-serif font. The background of the slide is a light gray gradient with a network diagram of nodes and lines at the bottom.

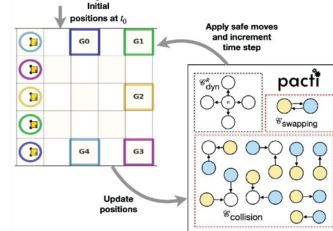
Inigo Incer et al.: Pacti: Scaling assume-guarantee reasoning for system analysis and design. arXiv:2303.17751 2023. Under review.

6

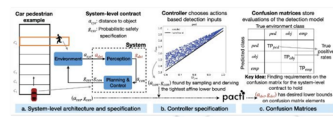
## CPS



### Space missions

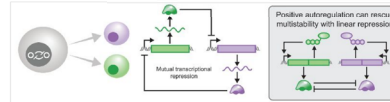


### Multi-agent planning



### Perception in autonomous vehicles

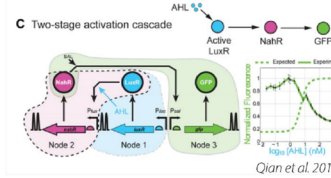
## Synthetic Biology



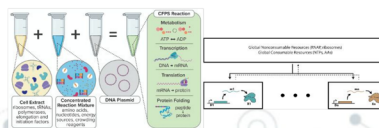
### Mammalian cell toggle-switch



### Resource competition in CRISPR



### Sequential signal processing in bacteria



### Cell-free biosensing

pacti  
.ORG

## Outline

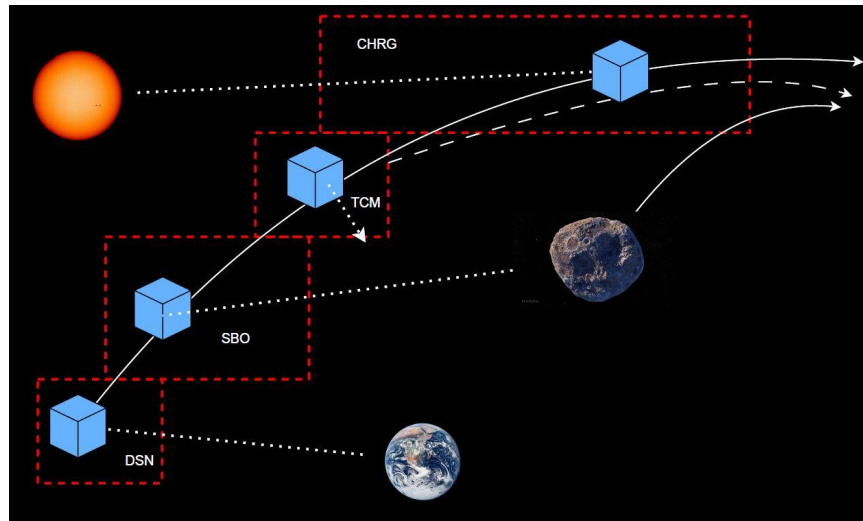
1. NASA JPL's space-mission case study
2. Quantifying the robustness of perception components
3. Theory of AG contracts
4. Conclusions

# Outline

1. NASA JPL's space-mission case study
2. Quantifying the robustness of perception components
3. Theory of AG contracts
4. Conclusions



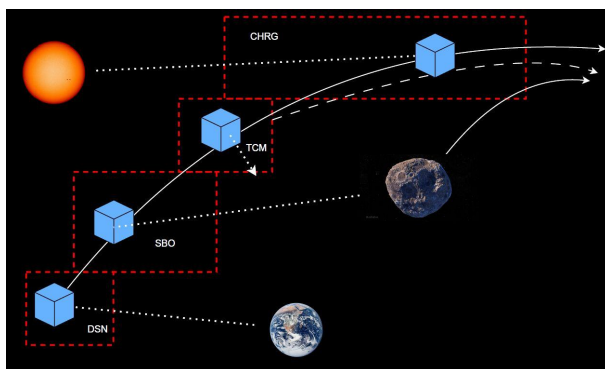
# Designing a space mission



Nicolas Rouquette, Inigo Incer, Alessandro Pinto. Early Design Exploration of Space System Scenarios Using Assume-Guarantee Contracts. IEEE SMC-IT 2023.

11

# Designing a spacecraft for a mission



Given  $n$  repetitions of the 4 scenario tasks:

$DSN_1, SBO_1, TCM_1, CHRGR_1, \dots, CHRGR_n, TCM_n, CHRGR_{n+1}$

Q1. Can the spacecraft maintain adequate power throughout?

Q2. Can the spacecraft record and transmit all asteroid observations?

12

# Current design processes

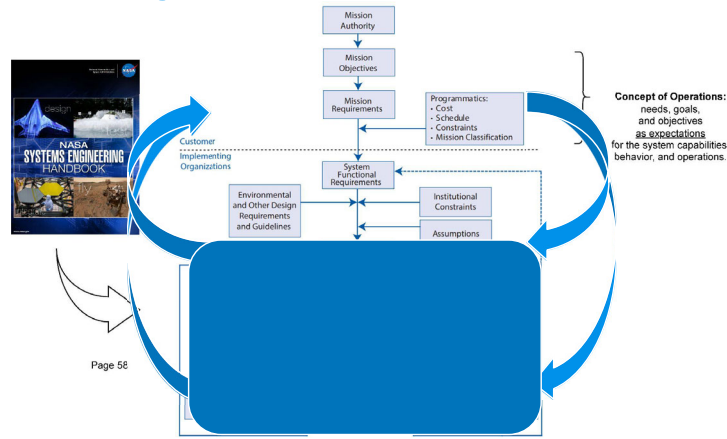


FIGURE 4.2-3 The Flowdown of Requirements  
<https://www.nasa.gov/connect/ebooks/nasa-systems-engineering-handbook>

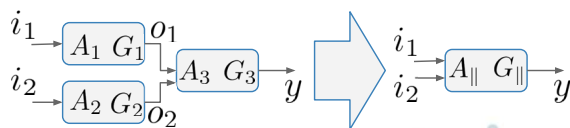
# Assume-guarantee contracts

- We will represent all components in a system using **assume-guarantee contracts**
- Contracts are formal specifications stating
  - (i) what a component does and
  - (ii) what it expects from its environment in order to deliver its guarantees
- Contracts have notion of order
- They have many system-relevant operations

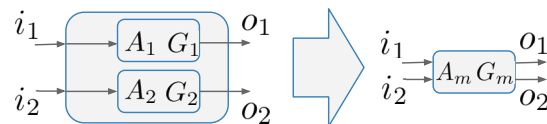
Contract = (assumptions, guarantees)

Eg:  
 (at most 30% of location sensors are attacked, the self-driving car reaches its goal with at least 99% chance)

## Building systems



## Merging viewpoints

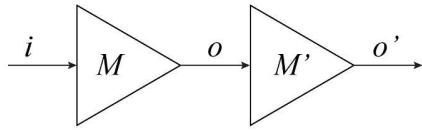


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Roberto Passerone, Inigo Incer, Alberto L. Sangiovanni-Vincentelli: Coherent Extension, Composition, and Merging Operators in Contract Models for System Design. ACM TECS 2019.

# Composition example



$$C = (|i| \leq 2, o = i) \quad C' = (|o| \leq 1, o' = o)$$

$$C_S = (|i| \leq 1, o' = i)$$



```

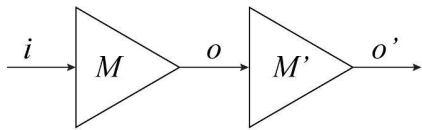
1 contract1 = PolyhedralContract.from_string(
2     input_vars=["i"],
3     output_vars=["o"],
4     assumptions=["|i| <= 2"],
5     guarantees=["o - i = 0"]
6 )
7
8 contract2 = PolyhedralContract.from_string(
9     input_vars=["o"],
10    output_vars=["o_p"],
11    assumptions=["|o| <= 1"],
12    guarantees=["o_p - o = 0"]
13 )
14
15 system_contract = contract1.compose(contract2)
16 print(system_contract)

```

✓ 0.1s

InVars: [i]  
 OutVars: [o\_p]  
 A: [  
   |i| <= 1  
 ]  
 G: [  
   -i + o\_p = 0  
 ]

# Diagnostics example



$$C = (|i| \leq 2, |o| \leq 3) \quad C' = (|o| \leq 1, o' = o)$$

System has an interconnection problem that **simulation is not guaranteed to catch**



```

1 contract1 = PolyhedralIoContract.from_strings(
2     input_vars=["i"],
3     output_vars=["o"],
4     assumptions=["|i| <= 2"],
5     guarantees=["|o| <= 3"]
6 )
7
8 contract2 = PolyhedralIoContract.from_strings(
9     input_vars=["o"],
10    output_vars=["o_p"],
11    assumptions=["|o| <= 1"],
12    guarantees=["o_p = o"]
13 )
14
15 try:
16     system_contract = contract1.compose(contract2)
17 except ValueError as e:
18     print("Composition error: {}".format(e))

```

✓ 0.0s

Composition error: Could not eliminate variables ['o', 'o\_p'] by refining the assumptions

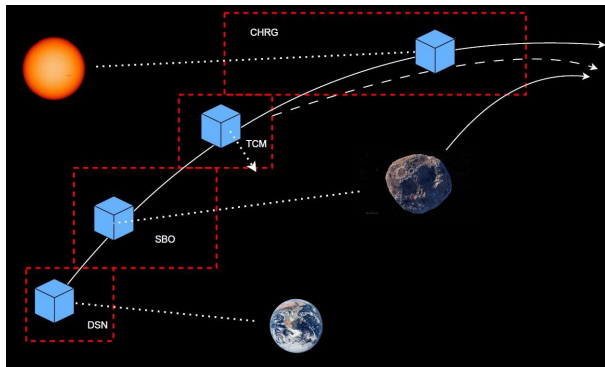
```

[
  |o| <= 1
]
using guarantees
[
  |i| <= 2
  |o| <= 3
]

```



# Designing a spacecraft for a mission I



Given  $n$  repetitions of the 4 scenario tasks:

$DSN_1, SBO_1, TCM_1, CHR_{1,}, \dots, CHR_n,$   
 $TCM_n, CHR_{n+1}$

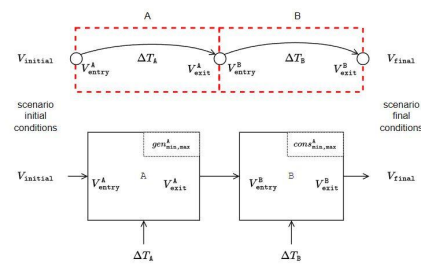
Q1. Can the spacecraft maintain adequate **power** throughout?

Q2. Can the spacecraft record and transmit all **asteroid observations**?

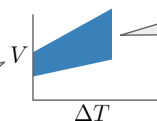


# Designing a spacecraft for a mission II

- The questions generate state variables:
  - state of charge
  - scientific data gathered
  - data transmitted to earth
  - relative distance to SBO
- Each mode of operation makes guarantees on each state (viewpoint)



Assumptions: acceptable initial values for state

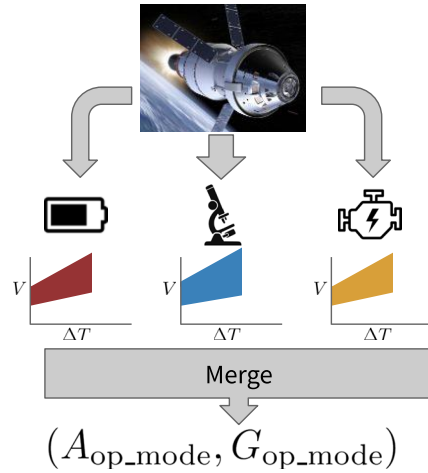


Guarantees: range of output state values (time-dependent)



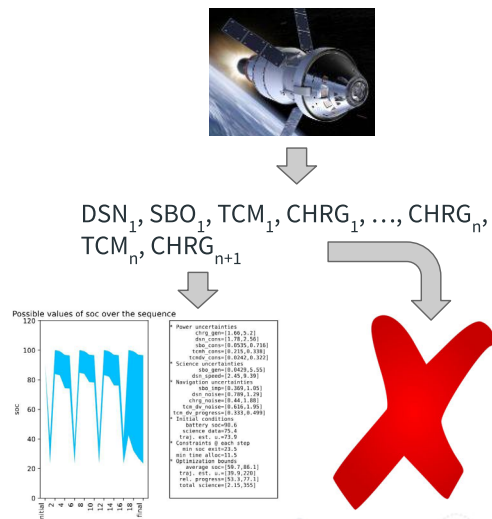
# Designing a spacecraft for a mission III

- Each spacecraft design has a contract for each viewpoint (power, distance to objective, etc.)
- To get the contract of every mode of operation, we merge its viewpoints
  - Each mode of operation makes guarantees of each state
  - And makes assumptions on initial state



# Designing a spacecraft for a mission IV

- For each spacecraft, we can ask whether the mission can be accomplished by composing the contracts in the schedule
- If the composition of contracts is successful, the spacecraft can complete the mission



# Efficiently designing a spacecraft for a mission



- We considered 200 spacecraft configurations and schedules of 5 and 20 steps
- The analysis for each spacecraft was recomputed by varying the top-level requirements
  - 200 configurations and 100 variations of requirements

Scenario	Pacti operations for scenario generation
5-step	compose: 2016, up to 22 constraints, 12 variables merge: 1680, up to 44 constraints, 23 variables total time: 16.3 seconds
20-step	compose: 10,200, up to 187 constraints, 95 variables merge: 8,000, up to 44 constraints, 23 variables total time: 97.8 seconds

Scenario	Pacti operations for schedulability analysis
5-step	merge: 181,988, up to 81 constraints, 35 variables admissible solutions: 401 out of 20,000 combinations total time: 3 minutes, 9.6 seconds
20-step	merge: 781,331, up to 275 constraints, 125 variables admissible solutions: 244 out of 20,000 combinations total time: 4 minutes, 11 seconds

## Current design processes

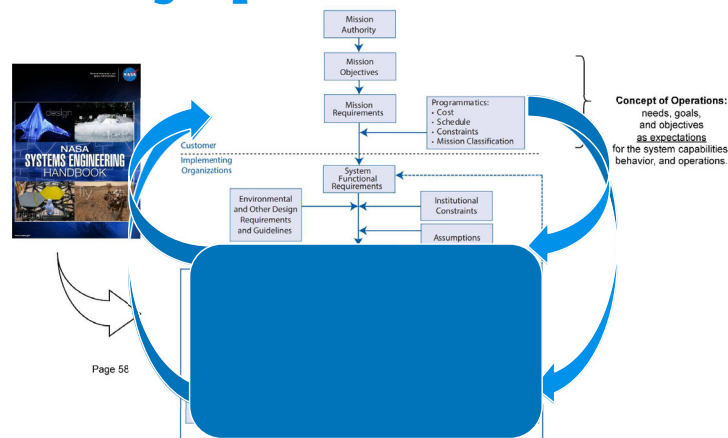
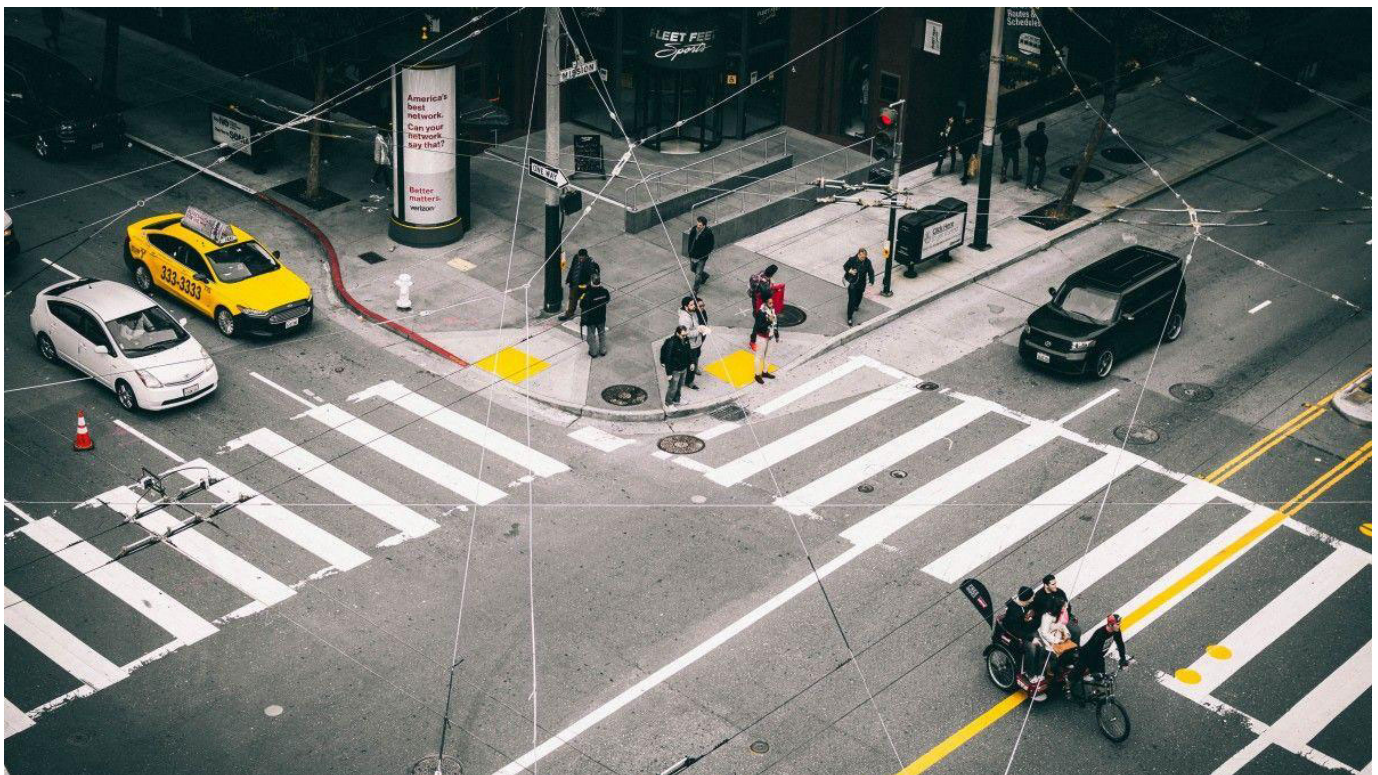


FIGURE 4.2-3 The Flowdown of Requirements  
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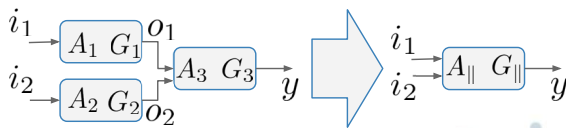


# Assume-guarantee contracts

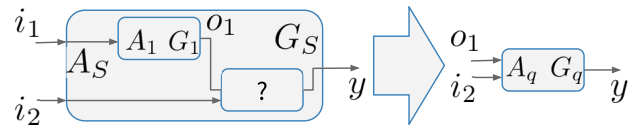
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- Contracts are formal specifications stating
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- They have many system-relevant operations:

$$C = (A, G)$$

## Building systems



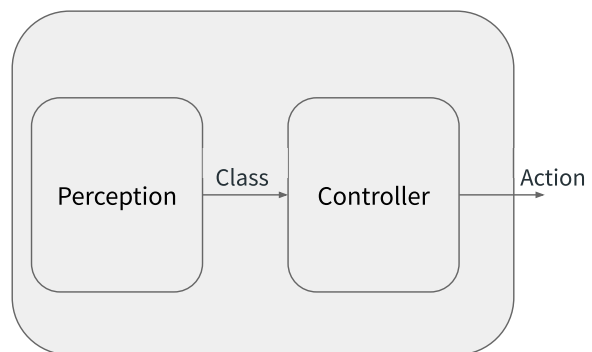
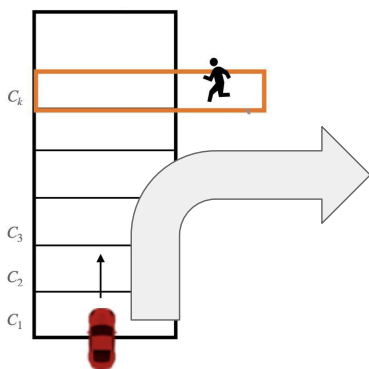
## Decomposing systems



Inigo Incer, Alberto Sangiovanni-Vincentelli, Chung-Wei Lin, Eunsuk Kang. Quotient for Assume-Guarantee Contracts. MEMOCODE 2018.

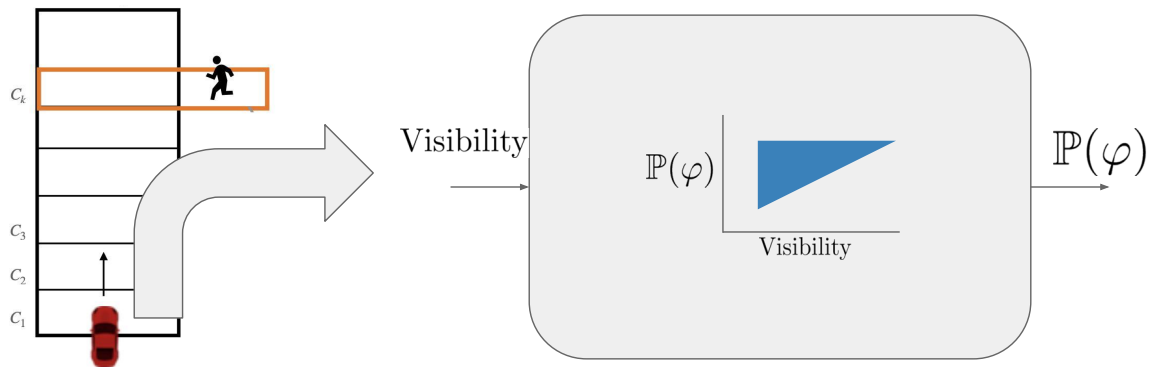
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# Deriving perception requirements

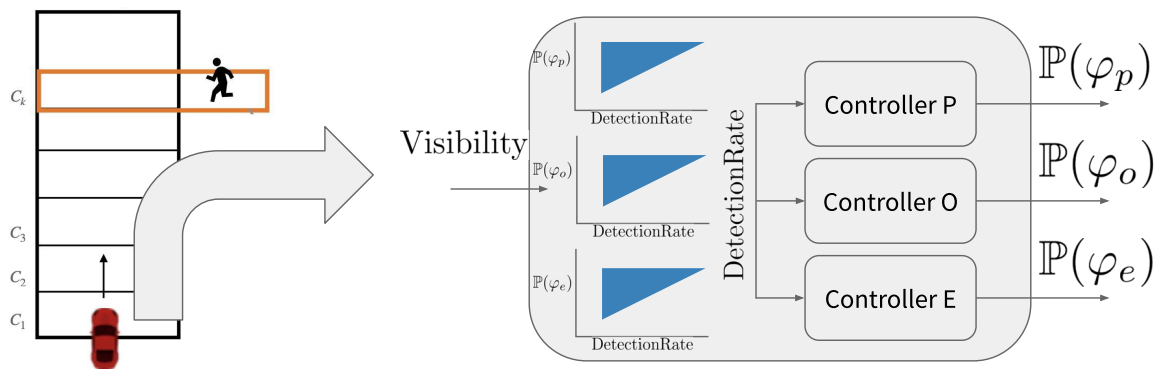


26

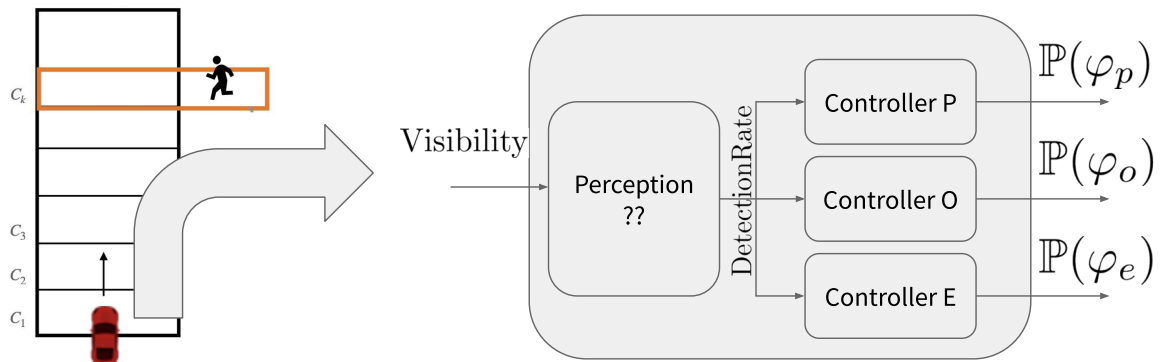
# Deriving perception requirements



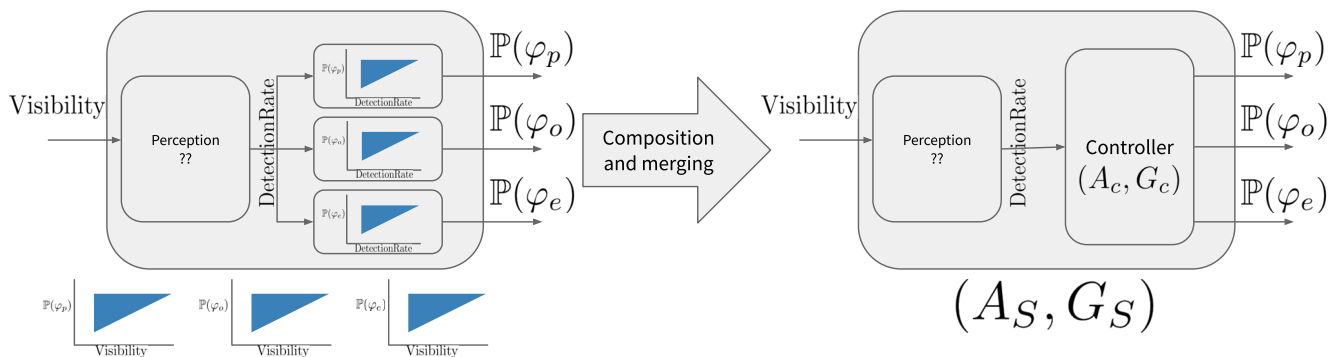
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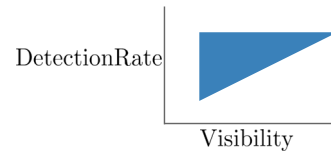
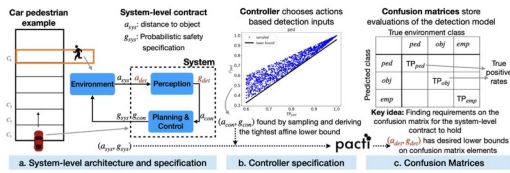
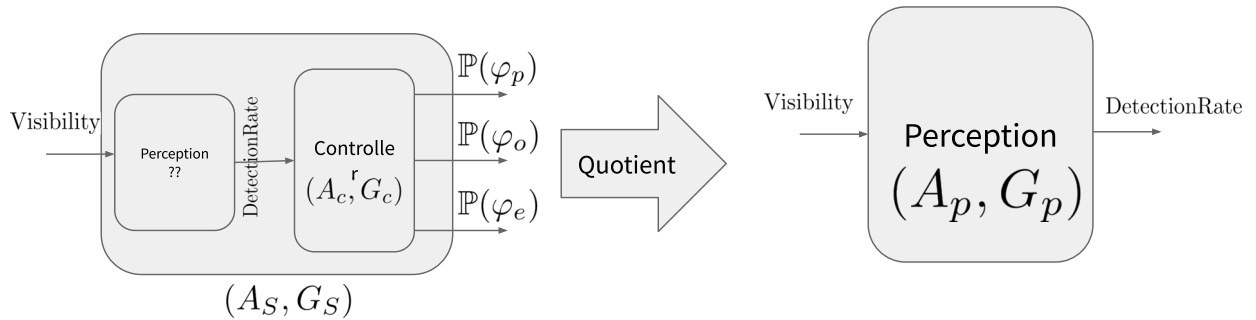
# Deriving perception requirements



# Deriving perception requirements



# Deriving perception requirements



31

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32



# The algebra of AG contracts

- Given a Boolean algebra  $B$  of specifications
- Its contract algebra is the set

$$\mathbb{C}(B) = \{(a, g) \in B^{\text{op}} \times B \mid a \vee g = 1_B\}$$

Constraint ensures that guarantees are SAT when assumptions are UNSAT

- Contracts have the following order

$$(a, g) \leq (a', g') \text{ iff } (g \leq g') \wedge (a' \leq a)$$

- The unary operation of reciprocal

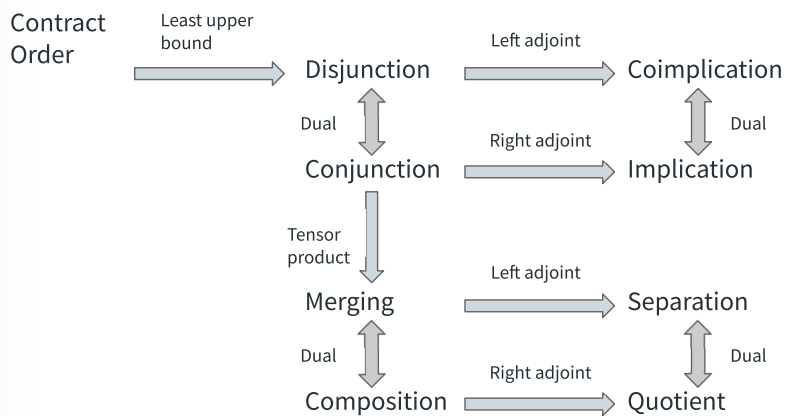
$$(a, g)^{-1} = (g, a)$$

- Enables the definition of duality of operations

$$(\mathcal{C} \circ \mathcal{C}')^{-1} = \mathcal{C}^{-1} \diamond (\mathcal{C}')^{-1}$$



## Contract operations I



# Contract operations II

Conjunction

$$\mathcal{C} \wedge \mathcal{C}' = (a \vee a', g \wedge g')$$

Composition

$$\mathcal{C}_1 \parallel \mathcal{C}_2 = (a_1 \wedge a_2 \vee \neg(g_1 \wedge g_2), g_1 \wedge g_2)$$

Quotient

$$\mathcal{C}/\mathcal{C}' = (a \wedge g', g \wedge a' \vee \neg(a \wedge g'))$$

Implication

$$\mathcal{C}' \rightarrow \mathcal{C} = ((a \wedge \neg a') \vee (g' \wedge \neg g), g \vee \neg g')$$

Disjunction

$$\mathcal{C} \vee \mathcal{C}' = (a \wedge a', g \vee g')$$

Merging

$$\mathcal{C}_1 \bullet \mathcal{C}_2 = (a_1 \wedge a_2, g_1 \wedge g_2 \vee \neg(a_1 \wedge a_2))$$

Separation

$$\mathcal{C} \div \mathcal{C}' = (a \wedge g' \vee \neg(g \wedge a'), g \wedge a')$$

Coimplication

$$\mathcal{C}' \nrightarrow \mathcal{C} = (a \vee \neg a', (g \wedge \neg g') \vee (a' \wedge \neg a))$$



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## What do we gain with contracts?

- We think of systems and subsystems in terms of their specifications—not implementation details
  - Conclusions will hold for any implementation adhering to its specification
- Contracts make assumptions first-class elements—we have to explicitly state the assumptions of all components
  - Operating on assumptions is less intuitive than on guarantees
- AG contracts enable us to scale compositional reasoning to large designs
  - The algebra has several design-relevant operations
- Contracts add logical AG reasoning to our system-level analysis; they don't replace our specialized tools
  - Contracts use control-theoretic tools to reason about control specifications, security tools to reason about security specifications, etc.

